

Package ‘ftsa’

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Description Functions for functional time series

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ftsa-package

*Functional time series analysis***Description**

This package presents descriptive statistics for modeling functional data; implements principal component regression and partial least squares regression to provide point and distributional forecasts for functional data; utilizes ordinary least squares, penalized least squares, ridge regression, and moving block approaches to dynamically update point and distributional forecasts when partial data points in the most recent curve are observed.

Author(s)

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References

R. J. Hyndman and H. L. Shang (2009) "Forecasting functional time series (with discussion)", *Journal of the Korean Statistical Society*, **38**(3), 199-221.

R. J. Hyndman and H. L. Shang. (2010) "Rainbow plots, bagplots, and boxplots for functional data", *Journal of Computational and Graphical Statistics*, **19**(1), 29-45.

H. L. Shang and R. J. Hyndman (2011) "Nonparametric time series forecasting with dynamic updating", *Mathematics and Computers in Simulation*, **81**(7), 1310-1324.

H. L. Shang, H. Booth and R. J. Hyndman (2011) "Point and interval forecasts of mortality rates and life expectancy: a comparison of ten principal component methods", *Demographic Research*, **25**(5), 173-214.

centre	<i>Mean function, variance function, median function, trim mean function of functional data</i>
--------	-------------------------------------------------------------------------------------------------

Description

Mean function, variance function, median function, trim mean function of functional data

Usage

```
centre(x, type)
```

Arguments

x	An object of class <code>matrix</code> .
type	Mean, variance, median or trim mean?

Value

Return mean function, variance function, median function or trim mean function.

Author(s)

Han Lin Shang

See Also

[pcscorebootstrapdata](#)

Examples

```
centre(ElNino$y, "mean")
```

diff.fts

Differences of a functional time series

Description

Computes differences of a fts object at each variable.

Usage

```
## S3 method for class 'fts'  
diff(x, lag = 1, differences = 1, ...)
```

Arguments

x	An object of class fts.
lag	An integer indicating which lag to use.
differences	An integer indicating the order of the difference.
...	Other arguments.

Value

An object of class fts.

Author(s)

Rob J Hyndman

Examples

```
diff(x = ElNino)
```

dynupdate*Dynamic updates via BM, OLS, RR and PLS methods*

Description

Four methods, namely block moving (BM), ordinary least squares (OLS) regression, ridge regression (RR), penalized least squares (PLS) regression, were proposed to address the problem of dynamic updating, when partial data in the most recent curve are observed.

Usage

```

dynupdate(data, newdata = NULL, holdoutdata, method = c("ts", "block",
"ols", "pls", "ridge"), fmethod = c("arima", "ar", "ets", "ets.na",
"rwdrift", "rw"), pcdmethod = c("classical", "M", "rapca"),
ngrid = max(1000, ncol(data$y)), order = 6, lambda = 0.01,
value = FALSE, interval = FALSE, level = 80,
pimethod = c("parametric", "nonparametric"), B = 1000)

```

Arguments

<code>data</code>	An object of class <code>sfts</code> .
<code>newdata</code>	A data vector of newly arrived observations.
<code>holdoutdata</code>	A data vector of holdout sample to evaluate point forecast accuracy.
<code>method</code>	Forecasting methods. The latter four can dynamically update point forecasts.
<code>fmethod</code>	Univariate time series forecasting methods used in <code>method = "ts"</code> or <code>method = "block"</code> .
<code>pcdmethod</code>	Method to use for principal components decomposition. Possibilities are "M", "rapca" and "classical".
<code>ngrid</code>	Number of grid points to use in calculations. Set to maximum of 1000 and <code>ncol(data\$y)</code> .
<code>order</code>	Number of principal components to fit.
<code>lambda</code>	Penalty parameter used in <code>method = "pls"</code> .
<code>value</code>	When <code>value = TRUE</code> , returns forecasts or when <code>value = FALSE</code> , returns forecast errors.
<code>interval</code>	When <code>interval = TRUE</code> , produces distributional forecasts.
<code>level</code>	Nominal coverage probability.
<code>pimethod</code>	Parametric or nonparametric method to construct prediction intervals.
<code>B</code>	Number of bootstrap samples.

Details

This function is designed to dynamically update point and distributional forecasts, when partial data in the most recent curve are observed.

If `method = "classical"`, then standard functional principal component decomposition is used, as described by Ramsay and Dalzell (1991).

If `method = "rapca"`, then the robust principal component algorithm of Hubert, Rousseeuw and Verboven (2002) is used.

If `method = "M"`, then the hybrid algorithm of Hyndman and Ullah (2005) is used.

Value

<code>forecasts</code>	An object of class <code>fsts</code> containing the dynamic updated point forecasts.
<code>bootsamp</code>	An object of class <code>fsts</code> containing the bootstrapped point forecasts, which are updated by the PLS method.
<code>low</code>	An object of class <code>fsts</code> containing the lower bound of prediction intervals.
<code>up</code>	An object of class <code>fsts</code> containing the upper bound of prediction intervals.

Author(s)

Han Lin Shang

References

- J. O. Ramsay and C. J. Dalzell (1991) "Some tools for functional data analysis (with discussion)", *Journal of the Royal Statistical Society: Series B*, **53**(3), 539-572.
- M. Hubert and P. J. Rousseeuw and S. Verboven (2002) "A fast robust method for principal components with applications to chemometrics", *Chemometrics and Intelligent Laboratory Systems*, **60**(1-2), 101-111.
- R. J. Hyndman and M. S. Ullah (2007) "Robust forecasting of mortality and fertility rates: A functional data approach", *Computational Statistics and Data Analysis*, **51**(10), 4942-4956.
- H. Shen and J. Z. Huang (2008) "Interday forecasting and intraday updating of call center arrivals", *Manufacturing and Service Operations Management*, **10**(3), 391-410.
- H. Shen (2009) "On modeling and forecasting time series of curves", *Technometrics*, **51**(3), 227-238.
- H. L. Shang and R. J. Hyndman (2011) "Nonparametric time series forecasting with dynamic updating", *Mathematics and Computers in Simulation*, **81**(7), 1310-1324.

See Also

[ftsm](#), [forecast.ftsm](#), [plot.ftsm](#), [residuals.ftsm](#), [summary.ftsm](#)

Examples

```
dynupdate(data = ElNino, newdata = ElNino$y[1:4,57],
           holdoutdata = ElNino$y[5:12,57], method = "ts")
dynupdate(data = ElNino, newdata = ElNino$y[1:4,57],
           holdoutdata = ElNino$y[5:12,57], method = "block")
dynupdate(data = ElNino, newdata = ElNino$y[1:4,57],
           holdoutdata = ElNino$y[5:12,57], method = "ols")
dynupdate(data = ElNino, newdata = ElNino$y[1:4,57],
           holdoutdata = ElNino$y[5:12,57], method = "pls")
dynupdate(data = ElNino, newdata = ElNino$y[1:4,57],
           holdoutdata = ElNino$y[5:12,57], method = "ridge")
dynupdate(data = ElNino, newdata = ElNino$y[1:4,57],
           holdoutdata = ElNino$y[5:12,57], method = "block", interval = TRUE)
```

error

Forecast error measure

Description

Computes the forecast error measure.

Usage

```
error(forecast, forecastbench, true, method = c("me", "mpe", "mae",
"mse", "sse", "rmse", "mdae", "mdse", "mape", "mdape", "smape",
"smdape", "rmspe", "rmdspe", "mrae", "mdrae", "gmrae",
"relmae", "relmse", "mase", "mdase", "rmsse"), giveall = FALSE)
```

Arguments

forecast	Forecasted values.
forecastbench	Forecasted values using a benchmark method, such as random walk.
true	Observed values.
method	Method of forecast error measure.
giveall	If giveall = TRUE, all error measures are provided.

Details***Bias measure:***

If method = "me", the forecast error measure is mean error.

If method = "mpe", the forecast error measure is mean percentage error.

Forecast accuracy error measure:

If method = "mae", the forecast error measure is mean absolute error.

If method = "mse", the forecast error measure is mean square error.

If method = "sse", the forecast error measure is sum square error.

If method = "rmse", the forecast error measure is root mean square error.

If method = "mdae", the forecast error measure is median absolute error.

If method = "mape", the forecast error measure is mean absolute percentage error.

If method = "mdape", the forecast error measure is median absolute percentage error.

If method = "rmspe", the forecast error measure is root mean square percentage error.

If method = "rmdspe", the forecast error measure is root median square percentage error.

Forecast accuracy symmetric error measure:

If method = "smape", the forecast error measure is symmetric mean absolute percentage error.

If method = "smdape", the forecast error measure is symmetric median absolute percentage error.

Forecast accuracy relative error measure:

If method = "mrae", the forecast error measure is mean relative absolute error.

If method = "mdrae", the forecast error measure is median relative absolute error.

If method = "gmrae", the forecast error measure is geometric mean relative absolute error.

If method = "relmae", the forecast error measure is relative mean absolute error.

If method = "relmse", the forecast error measure is relative mean square error.

Forecast accuracy scaled error measure:

If method = "mase", the forecast error measure is mean absolute scaled error.

If method = "mdase", the forecast error measure is median absolute scaled error.

If method = "rmsse", the forecast error measure is root mean square scaled error.

Value

A numeric value.

Author(s)

Han Lin Shang

References

P. A. Thompson (1990) "An MSE statistic for comparing forecast accuracy across series", *International Journal of Forecasting*, **6**(2), 219-227.

C. Chatfield (1992) "A commentary on error measures", *International Journal of Forecasting*, **8**(1), 100-102.

S. Makridakis (1993) "Accuracy measures: theoretical and practical concerns", *International Journal of Forecasting*, **9**(4), 527-529.

R. J. Hyndman and A. Koehler (2006) "Another look at measures of forecast accuracy", *International Journal of Forecasting*, **22**(3), 443-473.

Examples

```
error(forecast = 1:2, true = 3:4, method = "mae")
error(forecast = 1:2, true = 3:4, method = "mse")
error(forecast = 1:5, forecastbench = 6:10, true = 11:15, method = "mrae")
error(forecast = 1:5, forecastbench = 6:10, true = 11:15, method = "mdrae")
```

extract

Extract variables or observations

Description

Creates subsets of a fts object.

Usage

```
extract(data, direction = c("time", "x"), timeorder, xorder)
```

Arguments

data	An object of fts.
direction	In time direction or x variable direction?
timeorder	Indexes of time order.
xorder	Indexes of x variable order.

Value

When `xorder` is specified, it returns a `fts` object with same argument as `data` but with a subset of `x` variables.

When `timeorder` is specified, it returns a `fts` object with same argument as `data` but with a subset of time variables.

Author(s)

Han Lin Shang

Examples

```
extract(ElNino, direction = "time", timeorder = 1980:2006) # Last 27 curves
extract(ElNino, direction = "x", xorder = 1:8) # First 8 x variables
```

fbootstrap

Bootstrap independent and identically distributed functional data

Description

Computes bootstrap or smoothed bootstrap samples based on independent and identically distributed functional data.

Usage

```
fbootstrap(data, estad = func.mean, alpha = 0.05, nb = 200, suav = 0,
  media.dist = FALSE, graph = FALSE, ...)
```

Arguments

<code>data</code>	An object of class <code>fds</code> or <code>fts</code> .
<code>estad</code>	Estimate function of interest. Default is to estimate the mean function. Other options are <code>func.mode</code> or <code>func.var</code> .
<code>alpha</code>	Significance level used in the smooth bootstrapping.
<code>nb</code>	Number of bootstrap samples.
<code>sua</code>	Smoothing parameter.
<code>media.dist</code>	Estimate mean function.
<code>graph</code>	Graphical output.
<code>...</code>	Other arguments.

Value

A list containing the following components is returned.

estimate	Estimate function.
max.dist	Max distance of bootstrap samples.
rep.dist	Distances of bootstrap samples.
resamples	Bootstrap samples.
center	Functional mean.

Author(s)

Han Lin Shang

References

A. Cuevas and M. Febrero and R. Fraiman (2006), "On the use of the bootstrap for estimating functions with functional data", *Computational Statistics and Data Analysis*, **51**(2), 1063-1074.

M. Febrero and P. Galeano and W. Gonzalez-Manteiga (2007) "A functional analysis of NOx levels: location and scale estimation and outlier detection", *Computational Statistics*, **22**(3), 411-427.

M. Febrero and P. Galeano and W. Gonzalez-Manteiga (2008) "Outlier detection in functional data by depth measures, with application to identify abnormal NOx levels", *Environmetrics*, **19**(4), 331-345.

M. Febrero and P. Galeano and W. Gonzalez-Manteiga (2010) "Measures of influence for the functional linear model with scalar response", *Journal of Multivariate Analysis*, **101**(2), 327-339.

See Also

[pcscorebootstrapdata](#)

Examples

```
fbootstrap(data = ElNino)
```

forecast.ftsm

Forecast functional time series

Description

The coefficients from the fitted object are forecasted using either an ARIMA model (method = "arima"), an AR model (method = "ar"), an exponential smoothing method (method = "ets"), a linear exponential smoothing method allowing missing values (method = "ets.na"), or a random walk with drift model (method = "rwdrift"). The forecast coefficients are then multiplied by the principal components to obtain a forecast curve.

Usage

```
## S3 method for class 'ftsm'
forecast(object, h = 10, method = c("ets", "arima", "ar", "ets.na",
  "rwdrift", "rw", "struct", "arfima"), level = 80, jumpchoice = c("fit",
  "actual"), pimethod = c("parametric", "nonparametric"), B = 100,
  usedata = nrow(object$coeff), adjust = TRUE, model = NULL,
  damped = NULL, stationary = FALSE, ...)
```

Arguments

object	Output from <code>ftsm</code> .
h	Forecast horizon.
method	Univariate time series forecasting methods. Current possibilities are “ets”, “arima”, “ets.na”, “rwdrift” and “rw”.
level	Coverage probability of prediction intervals.
jumpchoice	Jump-off point for forecasts. Possibilities are “actual” and “fit”. If “actual”, the forecasts are bias-adjusted by the difference between the fit and the last year of observed data. Otherwise, no adjustment is used. See Booth et al. (2006) for the detail on jump-off point.
pimethod	Indicates if parametric method is used to construct prediction intervals.
B	Number of bootstrap samples.
usedata	Number of time periods to use in forecasts. Default is to use all.
adjust	If <code>adjust = TRUE</code> , adjusts the variance so that the one-step forecast variance matches the empirical one-step forecast variance.
model	If the ets method is used, <code>model</code> allows a model specification to be passed to <code>ets()</code> .
damped	If the ets method is used, <code>damped</code> allows the damping specification to be passed to <code>ets()</code> .
stationary	If <code>stationary = TRUE</code> , <code>method</code> is set to <code>method = "ar"</code> and only stationary AR models are used.
...	Other arguments passed to forecast routine.

Details

1. Obtain a smooth curve $f_t(x)$ for each t using a nonparametric smoothing technique.
2. Decompose the smooth curves via a functional principal component analysis.
3. Fit a univariate time series model to each of the principal component scores.
4. Forecast the principal component scores using the fitted time series models.
5. Multiply the forecast principal component scores by fixed principal components to obtain forecasts of $f_{n+h}(x)$.
6. The estimated variances of the error terms (smoothing error and model residual error) are used to compute prediction intervals for the forecasts.

Value

List with the following components:

mean	An object of class <code>fts</code> containing point forecasts.
lower	An object of class <code>fts</code> containing lower bound for prediction intervals.
upper	An object of class <code>fts</code> containing upper bound for prediction intervals.
fitted	An object of class <code>fts</code> of one-step-ahead forecasts for historical data.
error	An object of class <code>fts</code> of one-step-ahead errors for historical data.
coeff	List of objects of type <code>forecast</code> containing the coefficients and their forecasts.
coeff.error	One-step-ahead forecast errors for each of the coefficients.
var	List containing the various components of variance: model, error, mean, total and coeff.
model	Fitted <code>ftsm</code> model.
bootsamp	An array of $dimension = c(p, B, h)$ containing the bootstrapped point forecasts. p is the number of variables. B is the number of bootstrap samples. h is the forecast horizon.

Author(s)

Rob J Hyndman

References

- H. Booth and R. J. Hyndman and L. Tickle and P. D. Jong (2006) "Lee-Carter mortality forecasting: A multi-country comparison of variants and extensions", *Demographic Research*, **15**, 289-310.
- B. Erbas and R. J. Hyndman and D. M. Gertig (2007) "Forecasting age-specific breast cancer mortality using functional data model", *Statistics in Medicine*, **26**(2), 458-470.
- R. J. Hyndman and M. S. Ullah (2007) "Robust forecasting of mortality and fertility rates: A functional data approach", *Computational Statistics and Data Analysis*, **51**(10), 4942-4956.
- R. J. Hyndman and H. Booth (2008) "Stochastic population forecasts using functional data models for mortality, fertility and migration", *International Journal of Forecasting*, **24**(3), 323-342.
- R. J. Hyndman and H. L. Shang (2009) "Forecasting functional time series" (with discussion), *Journal of the Korean Statistical Society*, **38**(3), 199-221.

See Also

[ftsm](#), [forecastfpls](#), [plot.ftsf](#), [plot.fm](#), [residuals.fm](#), [summary.fm](#)

Examples

```
forecast(object = ftsm(ElNino))
forecast(object = ftsm(ElNino, weight = TRUE))
```

forecastfpls	<i>Forecast functional time series</i>
--------------	----------------------------------------

Description

The decentralized response is forecasted by multiplying the estimated regression coefficient with the new decentralized predictor

Usage

```
forecastfpls(object, components = 2, h = 20)
```

Arguments

object	An object of class <code>fts</code> .
components	Number of optimal components.
h	Forecast horizon.

Value

A `fts` class object, containing forecasts of responses.

Author(s)

Han Lin Shang

References

R. J. Hyndman and H. L. Shang (2009) "Forecasting functional time series" (with discussion), *Journal of the Korean Statistical Society*, **38**(3), 199-221.

See Also

[forecast.ftsm](#), [ftsm](#), [plot.fm](#), [plot.ftsf](#), [residuals.fm](#), [summary.fm](#)

Examples

```
forecastfpls(Australiasmoothfertility, h = 5)
```

fplsr

*Functional partial least squares regression***Description**

Fits a functional partial least squares (PLSR) model using nonlinear partial least squares (NIPALS) algorithm or simple partial least squares (SIMPLS) algorithm.

Usage

```
fplsr(data, order = 6, type = c("simpls", "nipals"), unit.weights =
TRUE, weight = FALSE, beta = 0.1, interval = FALSE, method =
c("delta", "boota"), alpha = 0.05, B = 100, adjust = FALSE,
backh = 10)
```

Arguments

data	An object of class fts.
order	Number of principal components to fit.
type	When type = "nipals", uses the NIPALS algorithm; when type = "simpls", uses the SIMPLS algorithm.
unit.weights	Constrains predictor loading weights to have unit norm.
weight	When weight = TRUE, a set of geometrically decaying weights is applied to the decentralized data.
beta	When weight = TRUE, the speed of geometric decay is governed by a weight parameter.
interval	When interval = TRUE, produces distributional forecasts.
method	Method used for computing prediction intervals.
alpha	1-alpha gives the nominal coverage probability.
B	Number of replications.
adjust	When adjust = TRUE, an adjustment is performed.
backh	When adjust = TRUE, an adjustment is performed by evaluating the difference between predicted and actual values in a testing set. backh specifies the testing set.

Details***Point forecasts:***

The NIPALS function implements the orthogonal scores algorithm, as described in Martens and Naes (1989). This is one of the two classical PLSR algorithms, the other is the simple partial least squares regression in DeJong (1993). The difference between these two approaches is that the NIPALS deflates the original predictors and responses, while the SIMPLS deflates the covariance

matrix of original predictors and responses. Thus, SIMPLS is more computationally efficient than NIPALS.

In a functional data set, the functional PLSR can be performed by setting the functional responses to be 1 lag ahead of the functional predictors. This idea has been adopted from the Autoregressive Hilbertian processes of order 1 (ARH(1)) of Bosq (2000).

Distributional forecasts:

Parametric method:

Influenced by the works of Denham (1997) and Phatak et al. (1993), one way of constructing prediction intervals in the PLSR is via a local linearization method (also known as the Delta method). It can be easily understood as the first two terms in a Taylor series expansion. The variance of coefficient estimators can be approximated, from which an analytic-formula based prediction intervals are constructed.

Nonparametric method:

After discretizing and decentralizing functional data $f_t(x)$ and $g_s(y)$, a PLSR model with K latent components is built. Then, the fit residuals $o_s(y_i)$ between $g_s(y_i)$ and $\hat{g}_s(y_i)$ are calculated as

$$o_s(y_i) = g_s(y_i) - \hat{g}_s(y_i), i = 1, \dots, p.$$

The next step is to generate B bootstrap samples $o_s^b(y_i)$ by randomly sampling with replacement from $[o_1(y_i), \dots, o_n(y_i)]$. Adding bootstrapped residuals to the original response variables in order to generate new bootstrap responses,

$$g_s^b(y_i) = g_s(y_i) + o_s^b(y_i).$$

Then, the PLSR models are constructed using the centered and discretized predictors and bootstrapped responses to obtain the bootstrapped regression coefficients and point forecasts, from which the empirical prediction intervals and kernel density plots are constructed.

Value

A list containing the following components is returned.

B	$(p \times m)$ matrix containing the regression coefficients. p is the number of variables in the predictors and m is the number of variables in the responses.
P	$(p \times order)$ matrix containing the predictor loadings.
Q	$(m \times order)$ matrix containing the response loadings.
T	$(ncol(data\$y)-1) \times order$ matrix containing the predictor scores.
R	$(p \times order)$ matrix containing the weights used to construct the latent components of predictors.
Yscores	$(ncol(data\$y)-1) \times order$ matrix containing the response scores.
projection	$(p \times order)$ projection matrix used to convert predictors to predictor scores.
meanX	An object of class <code>f.ts</code> containing the column means of predictors.
meanY	An object of class <code>f.ts</code> containing the column means of responses.

Ypred	An object of class <code>fts</code> containing the 1-step-ahead predicted values of the responses.
fitted	An object of class <code>fts</code> containing the fitted values.
residuals	An object of class <code>fts</code> containing the regression residuals.
Xvar	A vector with the amount of predictor variance explained by each number of component.
Xtotvar	Total variance in predictors.
weight	When <code>weight = TRUE</code> , a set of geometrically decaying weights is given. When <code>weight = FALSE</code> , weights are all equal 1.
x1	Time period of a <code>fts</code> object, which can be obtained from <code>colnames(data\$y)</code> .
y1	Variables of a <code>fts</code> object, which can be obtained from <code>data\$x</code> .
ypred	Returns the original functional predictors.
y	Returns the original functional responses.
bootsamp	Bootstrapped point forecasts.
lb	Lower bound of prediction intervals.
ub	Upper bound of prediction intervals.
lbadj	Adjusted lower bound of prediction intervals.
ubadj	Adjusted upper bound of prediction intervals.
lbadjfactor	Adjusted lower bound factor, which lies generally between 0.9 and 1.1.
ubadjfactor	Adjusted upper bound factor, which lies generally between 0.9 and 1.1.

Author(s)

Han Lin Shang

References

- S. Wold and A. Ruhe and H. Wold and W. J. Dunn (1984) "The collinearity problem in linear regression. The partial least squares (PLS) approach to generalized inverses", *SIAM Journal of Scientific and Statistical Computing*, **5**(3), 735-743.
- S. de Jong (1993) "SIMPLS: an alternative approach to partial least square regression", *Chemometrics and Intelligent Laboratory Systems*, **18**(3), 251-263.
- C J. F. Ter Braak and S. de Jong (1993) "The objective function of partial least squares regression", *Journal of Chemometrics*, **12**(1), 41-54.
- B. Dayal and J. MacGregor (1997) "Recursive exponentially weighted PLS and its applications to adaptive control and prediction", *Journal of Process Control*, **7**(3), 169-179.
- B. D. Marx (1996) "Iteratively reweighted partial least squares estimation for generalized linear regression", *Technometrics*, **38**(4), 374-381.
- L. Xu and J-H. Jiang and W-Q. Lin and Y-P. Zhou and H-L. Wu and G-L. Shen and R-Q. Yu (2007) "Optimized sample-weighted partial least squares", *Talanta*, **71**(2), 561-566.
- A. Phatak and P. Reilly and A. Penlidis (1993) "An approach to interval estimation in partial least squares regression", *Analytica Chimica Acta*, **277**(2), 495-501.

M. Denham (1997) "Prediction intervals in partial least squares", *Journal of Chemometrics*, **11**(1), 39-52.

D. Bosq (2000) *Linear processes in function spaces*, New York: Springer.

N. Faber (2002) "Uncertainty estimation for multivariate regression coefficients", *Chemometrics and Intelligent Laboratory Systems*, **64**(2), 169-179.

J. A. Fernandez Pierna and L. Jin and F. Wahl and N. M. Faber and D. L. Massart (2003) "Estimation of partial least squares regression prediction uncertainty when the reference values carry a sizeable measurement error", *Chemometrics and Intelligent Laboratory Systems*, **65**(2), 281-291.

See Also

[ftsm](#), [forecast.ftsm](#), [plot.fm](#), [summary.fm](#), [residuals.fm](#), [plot.fmres](#)

Examples

```
fplsr(EINino, type = "nipals")
fplsr(EINino)
fplsr(EINino, weight = TRUE)
fplsr(EINino, unit.weights = FALSE)
fplsr(EINino, unit.weights = FALSE, weight = TRUE)
fplsr(EINino, interval = TRUE, method = "delta")
fplsr(EINino, interval = TRUE, method = "boota")
```

ftsm

Fit functional time series model

Description

Fits a principal component model to a `fts` object. The function uses optimal orthonormal principal components obtained from a principal components decomposition.

Usage

```
ftsm(y, order = 6, ngrid = max(500, ncol(y$y)), method = c("classical",
  "M", "rapca"), mean = TRUE, level = FALSE, lambda = 3,
  weight = FALSE, beta = 0.1, ...)
```

Arguments

<code>y</code>	An object of class <code>fts</code> .
<code>order</code>	Number of principal components to fit.
<code>ngrid</code>	Number of grid points to use in calculations. Set to maximum of 500 and <code>ncol(y\$y)</code> .
<code>method</code>	Method to use for principal components decomposition. Possibilities are "M", "rapca" and "classical".

mean	If mean = TRUE, it will estimate mean term in the model before computing basis terms. If mean = FALSE, the mean term is assumed to be zero.
level	If mean = TRUE, it will include an additional (intercept) term that depends on t but not on x .
lambda	Tuning parameter for robustness when method = "M".
weight	When weight = TRUE, a set of geometrically decaying weights is applied to the decentralized data.
beta	When weight = TRUE, the speed of geometric decay is governed by a weight parameter.
...	Additional arguments controlling the fitting procedure.

Details

If method = "classical", then standard functional principal component decomposition is used, as described by Ramsay and Dalzell (1991).

If method = "rapca", then the robust principal component algorithm of Hubert, Rousseeuw and Verboven (2002) is used.

If method = "M", then the hybrid algorithm of Hyndman and Ullah (2005) is used.

Value

Object of class "ftsm" with the following components:

x1	Time period of a fts object, which can be obtained from colnames(y\$y).
y1	Variables of a fts object, which can be obtained from y\$x.
y	Original functional time series or sliced functional time series.
basis	Matrix of principal components evaluated at value of y\$x (one column for each principal component). The first column is the fitted mean or median.
basis2	Matrix of principal components excluded from the selected model.
coeffs	Matrix of coefficients (one column for each coefficient series). The first column is all ones.
coeff2	Matrix of coefficients associated with the principal components excluded from the selected model.
fitted	An object of class fts containing the fitted values.
residuals	An object of class fts containing the regression residuals (difference between observed and fitted).
varprop	Proportion of variation explained by each principal component.
wt	Weight associated with each time period.
v	Measure of variation for each time period.
mean.se	Measure of standar error associated with the mean.

Author(s)

Rob J Hyndman

References

- J. O. Ramsay and C. J. Dalzell (1991) "Some tools for functional data analysis (with discussion)", *Journal of the Royal Statistical Society: Series B*, **53**(3), 539-572.
- M. Hubert and P. J. Rousseeuw and S. Verboven (2002) "A fast robust method for principal components with applications to chemometrics", *Chemometrics and Intelligent Laboratory Systems*, **60**(1-2), 101-111.
- B. Erbas and R. J. Hyndman and D. M. Gertig (2007) "Forecasting age-specific breast cancer mortality using functional data model", *Statistics in Medicine*, **26**(2), 458-470.
- R. J. Hyndman and M. S. Ullah (2007) "Robust forecasting of mortality and fertility rates: A functional data approach", *Computational Statistics and Data Analysis*, **51**(10), 4942-4956.
- R. J. Hyndman and H. Booth (2008) "Stochastic population forecasts using functional data models for mortality, fertility and migration", *International Journal of Forecasting*, **24**(3), 323-342.
- R. J. Hyndman and H. L. Shang (2009) "Forecasting functional time series (with discussion)", *Journal of the Korean Statistical Society*, **38**(3), 199-221.

See Also

[ftsmweightselect](#), [forecast.ftsm](#), [plot.fm](#), [plot.ftsf](#), [residuals.fm](#), [summary.fm](#)

Examples

```
ftsm(y = ElNino)
ftsm(y = ElNino, weight = TRUE)
```

ftsmiterativeforecasts

Forecast functional time series

Description

The coefficients from the fitted object are forecasted using either an ARIMA model (method = "arima"), an AR model (method = "ar"), an exponential smoothing method (method = "ets"), a linear exponential smoothing method allowing missing values (method = "ets.na"), or a random walk with drift model (method = "rwdrift"). The forecast coefficients are then multiplied by the principal components to obtain a forecast curve.

Usage

```
ftsmiterativeforecasts(object, components, iteration = 20)
```

Arguments

object	An object of class fts.
components	Number of principal components.
iteration	Number of iterative one-step-ahead forecasts.

Details

1. Obtain a smooth curve $f_t(x)$ for each t using a nonparametric smoothing technique.
2. Decompose the smooth curves via a functional principal component analysis.
3. Fit a univariate time series model to each of the principal component scores.
4. Forecast the principal component scores using the fitted time series models.
5. Multiply the forecast principal component scores by fixed principal components to obtain forecasts of $f_{n+h}(x)$.
6. The estimated variances of the error terms (smoothing error and model residual error) are used to compute prediction intervals for the forecasts.

Value

List with the following components:

mean	An object of class <code>fts</code> containing point forecasts.
lower	An object of class <code>fts</code> containing lower bound for prediction intervals.
upper	An object of class <code>fts</code> containing upper bound for prediction intervals.
fitted	An object of class <code>fts</code> of one-step-ahead forecasts for historical data.
error	An object of class <code>fts</code> of one-step-ahead errors for historical data.
coeff	List of objects of type <code>forecast</code> containing the coefficients and their forecasts.
coeff.error	One-step-ahead forecast errors for each of the coefficients.
var	List containing the various components of variance: model, error, mean, total and coeff.
model	Fitted <code>ftsm</code> model.
bootsamp	An array of $dim = c(p, B, h)$ containing the bootstrapped point forecasts. p is the number of variables. B is the number of bootstrap samples. h is the forecast horizon.

Author(s)

Han Lin Shang

References

- H. Booth and R. J. Hyndman and L. Tickle and P. D. Jong (2006) "Lee-Carter mortality forecasting: A multi-country comparison of variants and extensions", *Demographic Research*, **15**, 289-310.
- B. Erbas and R. J. Hyndman and D. M. Gertig (2007) "Forecasting age-specific breast cancer mortality using functional data model", *Statistics in Medicine*, **26**(2), 458-470.
- R. J. Hyndman and M. S. Ullah (2007) "Robust forecasting of mortality and fertility rates: A functional data approach", *Computational Statistics and Data Analysis*, **51**(10), 4942-4956.
- R. J. Hyndman and H. Booth (2008) "Stochastic population forecasts using functional data models for mortality, fertility and migration", *International Journal of Forecasting*, **24**(3), 323-342.
- R. J. Hyndman and H. L. Shang (2009) "Forecasting functional time series" (with discussion), *Journal of the Korean Statistical Society*, **38**(3), 199-221.

See Also

[ftsm](#), [plot.ftsf](#), [plot.fm](#), [residuals.fm](#), [summary.fm](#)

Examples

```
ftsmiterativeforecasts(Australiasmoothfertility, components = 2, iteration = 5)
```

ftsmweightselect	<i>Selection of the weight parameter used in the weighted functional time series model.</i>
------------------	---------------------------------------------------------------------------------------------

Description

The geometrically decaying weights are used to estimate the mean curve and functional principal components, where more weights are assigned to the more recent data than the data from the distant past.

Usage

```
ftsmweightselect(data, ncomp = 6, ntrainyear, errorcriterion = c("mae", "mse", "mape"))
```

Arguments

data	An object of class <code>fts</code> .
ncomp	Number of components.
ntrainyear	Number of holdout observations used to assess the forecast accuracy.
errorcriterion	Error measure.

Details

The data set is split into a fitting period and forecasting period. Using the data in the fitting period, we compute the one-step-ahead forecasts and calculate the forecast error. Then, we increase the fitting period by one, and carry out the same forecasting procedure until the fitting period covers entire data set. The forecast accuracy is determined by the averaged forecast error across the years in the forecasting period. By using an optimization algorithm, we select the optimal weight parameter that would result in the minimum forecast error.

Value

Optimal weight parameter.

Note

Can be computational intensive.

Author(s)

Han Lin Shang

References

R. J. Hyndman and H. L. Shang (2009) "Forecasting functional time series (with discussion)", *Journal of the Korean Statistical Society*, **38**(3), 199-221.

See Also

[ftsm](#), [forecast.ftsm](#)

Examples

```
ftsmweightselect(ElNinosmooth, ntrainyear = 1)
```

is.fts

Test for functional time series

Description

Tests whether an object is of class fts.

Usage

```
is.fts(x)
```

Arguments

x Arbitrary R object.

Author(s)

Rob J Hyndman

Examples

```
is.fts(x = ElNino)
```

isfe.fts

*Integrated Squared Forecast Error for models of various orders***Description**

Computes integrated squared forecast error (ISFE) values for functional time series models of various orders.

Usage

```
isfe.fts(data, max.order = N - 3, N = 10, h = 5:10, method =
c("classical", "M", "rapca"), mean = TRUE, level = FALSE,
fmethod = c("arima", "ar", "ets", "ets.na", "struct", "rwdrift",
"rw", "arfima"), lambda = 3, ...)
```

Arguments

data	An object of class fts.
max.order	Maximum number of principal components to fit.
N	Minimum number of functional observations to be used in fitting a model.
h	Forecast horizons over which to average.
method	Method to use for principal components decomposition. Possibilities are "M", "rapca" and "classical".
mean	Indicates if mean term should be included.
level	Indicates if level term should be included.
fmethod	Method used for forecasting. Current possibilities are "ets", "arima", "ets.na", "struct", "rwdrift" and "rw".
lambda	Tuning parameter for robustness when method = "M".
...	Additional arguments controlling the fitting procedure.

Value

Numeric matrix with $(\text{max.order}+1)$ rows and $\text{length}(h)$ columns containing ISFE values for models of orders $0:(\text{max.order})$.

Note

This function can be very time consuming for data with large dimensionality or large sample size. By setting `max.order` small, computational speed can be dramatically increased.

Author(s)

Rob J Hyndman

References

R. J. Hyndman and M. S. Ullah (2007) "Robust forecasting of mortality and fertility rates: A functional data approach", *Computational Statistics and Data Analysis*, **51**(10), 4942-4956.

See Also

[ftsm](#), [forecast.ftsm](#), [plot.fm](#), [plot.fmres](#), [summary.fm](#), [residuals.fm](#)

mean.fts

Mean functions for functional time series

Description

Computes mean of functional time series at each variable.

Usage

```
## S3 method for class 'fts'
mean(x, method = c("coordinate", "FM", "mode", "RP", "RPD"),
     na.rm = TRUE, ...)
```

Arguments

x	An object of class fts.
method	Method for computing the mean function.
na.rm	A logical value indicating whether NA values should be stripped before the computation proceeds.
...	Other arguments.

Details

If method = "coordinate", it computes the coordinate-wise functional mean.

If method = "FM", it computes the mean of trimmed functional data ordered by the functional depth of Fraiman and Muniz (2001).

If method = "mode", it computes the mean of trimmed functional data ordered by h -modal functional depth.

If method = "RP", it computes the mean of trimmed functional data ordered by random projection depth.

If method = "RPD", it computes the mean of trimmed functional data ordered by random projection derivative depth.

Value

A list containing x = variables and y = mean rates.

Author(s)

Rob J Hyndman, Han Lin Shang

References

O. Hossjer and C. Croux (1995) "Generalized univariate signed rank statistics for testing and estimating a multivariate location parameter", *Journal of Nonparametric Statistics*, **4**(3), 293-308.

A. Cuevas and M. Febrero and R. Fraiman (2006) "On the use of bootstrap for estimating functions with functional data", *Computational Statistics & Data Analysis*, **51**(2), 1063-1074.

M. Febrero and P. Galeano and W. Gonzalez-Manteiga (2008) "Outlier detection in functional data by depth measures, with application to identify abnormal NOx levels", *Environmetrics*, **19**(4), 331-345.

See Also

[median.fts](#), [var.fts](#), [sd.fts](#), [quantile.fts](#)

Examples

```
mean(x = ElNino, method = "coordinate")
mean(x = ElNino, method = "FM")
mean(x = ElNino, method = "mode")
mean(x = ElNino, method = "RP")
mean(x = ElNino, method = "RPD")
```

median

Median

Description

Generic function for the median.

Usage

```
median(...)
```

Arguments

... Arguments passed to specific methods.

Details

The [median](#) function in the stats package is replaced by `median.default`.

Value

Refer to specific methods. For numeric vectors, see the [median](#) function in the stats package.

Author(s)

Rob J Hyndman

See Also

[median.fts](#)

median.fts

Median functions for functional time series

Description

Computes median of functional time series at each variable.

Usage

```
## S3 method for class 'fts'  
median(x, method = c("hossjercroux", "coordinate", "FM", "mode",  
  "RP", "RPD"), ...)
```

Arguments

x	An object of class fts.
method	Method for computing median.
...	Other arguments.

Details

If method = "coordinate", it computes a coordinate-wise median.

If method = "hossjercroux", it computes the L1-median using the Hossjer-Croux algorithm.

If method = "FM", it computes the median of trimmed functional data ordered by the functional depth of Fraiman and Muniz (2001).

If method = "mode", it computes the median of trimmed functional data ordered by h -modal functional depth.

If method = "RP", it computes the median of trimmed functional data ordered by random projection depth.

If method = "RPD", it computes the median of trimmed functional data ordered by random projection derivative depth.

Value

A list containing x = variables and y = median rates.

Author(s)

Rob J Hyndman, Han Lin Shang

References

- O. Hossjer and C. Croux (1995) "Generalized univariate signed rank statistics for testing and estimating a multivariate location parameter", *Nonparametric Statistics*, **4**(3), 293-308.
- A. Cuevas and M. Febrero and R. Fraiman (2006) "On the use of bootstrap for estimating functions with functional data", *Computational Statistics & Data Analysis*, **51**(2), 1063-1074.
- M. Febrero and P. Galeano and W. Gonzalez-Manteiga (2008) "Outlier detection in functional data by depth measures, with application to identify abnormal NOx levels", *Environmetrics*, **19**(4), 331-345.

See Also

[mean.fts](#), [var.fts](#), [sd.fts](#), [quantile.fts](#)

Examples

```
median(x = ElNino, method = "hossjercroux")
median(x = ElNino, method = "coordinate")
median(x = ElNino, method = "FM")
median(x = ElNino, method = "mode")
median(x = ElNino, method = "RP")
median(x = ElNino, method = "RPD")
```

pcscorebootstrapdata *Bootstrap independent and identically distributed functional data or functional time series*

Description

Computes bootstrap or smoothed bootstrap samples based on either independent and identically distributed functional data or functional time series.

Usage

```
pcscorebootstrapdata(dat, bootrep, statistic, bootmethod = c("st", "sm", "mvn",
  "stiefel"), smo)
```

Arguments

dat	An object of class matrix.
bootrep	Number of bootstrap samples.
statistic	Summary statistics.
bootmethod	Bootstrap method. When bootmethod = "st", the sampling with replacement is implemented. To avoid the repeated bootstrap samples, the smoothed bootstrap method can be implemented by adding multivariate Gaussian random noise. When bootmethod = "mvn", the bootstrapped principal component scores are drawn from a multivariate Gaussian distribution with the mean and covariance

matrices of the original principal component scores. When `bootmethod = "stiefel"`, the bootstrapped principal component scores are drawn from a Stiefel manifold with the mean and covariance matrices of the original principal component scores.

`sno` Smoothing parameter.

Details

We will presume that each curve is observed on a grid of T points with $0 \leq t_1 < t_2 \dots < t_T \leq \tau$. Thus, the raw data set (X_1, X_2, \dots, X_n) of n observations will consist of an n by T data matrix. By applying the singular value decomposition, X_1, X_2, \dots, X_n can be decomposed into $X = ULR^T$, where the crossproduct of U and R is identity matrix.

Holding the mean and L and R fixed at their realized values, there are four re-sampling methods that differ mainly by the ways of re-sampling U .

(a) Obtain the re-sampled singular column matrix by randomly sampling with replacement from the original principal component scores.

(b) To avoid the appearance of repeated values in bootstrapped principal component scores, we adapt a smooth bootstrap procedure by adding a white noise component to the bootstrap.

(c) Because principal component scores follow a standard multivariate normal distribution asymptotically, we can randomly draw principal component scores from a multivariate normal distribution with mean vector and covariance matrix of original principal component scores.

(d) Because the crossproduct of U is identity matrix, U is considered as a point on the Stiefel manifold, that is the space of n orthogonal vectors, thus we can randomly draw principal component scores from the Stiefel manifold.

Value

`bootdata` Bootstrap samples. If the original data matrix is p by n , then the bootstrapped data are p by n by `bootrep`.

`meanfunction` Bootstrap summary statistics. If the original data matrix is p by n , then the bootstrapped summary statistics is p by `bootrep`.

Author(s)

Han Lin Shang

References

D. S. Poskitt and A. Sengarapillai (2012), "Description length and dimensionality reduction in functional data analysis", Computational Statistics and Data Analysis, in press.

See Also

[fbootstrap](#)

Examples

```
boot1 = pcscorebootstrapdata(ElNino$y, 500, "mean", bootmethod = "st")
boot2 = pcscorebootstrapdata(ElNino$y, 500, "mean", bootmethod = "sm", smo = 0.05)
boot3 = pcscorebootstrapdata(ElNino$y, 500, "mean", bootmethod = "mvn")
boot4 = pcscorebootstrapdata(ElNino$y, 500, "mean", bootmethod = "stiefel")
```

plot.fm

*Plot fitted model components for a functional model***Description**

When `class(x)[1] = ftsm`, plot showing the principal components in the top row of plots and the coefficients in the bottom row of plots.

When `class(x)[1] = fm`, plot showing the predictor scores in the top row of plots and the response loadings in the bottom row of plots.

Usage

```
## S3 method for class 'fm'
plot(x, order, xlab1 = x$y$name, ylab1 = "Principal component",
     xlab2 = "Time", ylab2 = "Coefficient", mean.lab = "Mean",
     level.lab = "Level", main.title = "Main effects", interaction.title
     = "Interaction", basiscol = 1, coeffcol = 1, outlier.col = 2,
     outlier.pch = 19, outlier.cex = 0.5, ...)
```

Arguments

<code>x</code>	Output from <code>ftsm</code> or <code>fplsr</code> .
<code>order</code>	Number of principal components to plot. Default is all principal components in a model.
<code>xlab1</code>	x-axis label for principal components.
<code>xlab2</code>	x-axis label for coefficient time series.
<code>ylab1</code>	y-axis label for principal components.
<code>ylab2</code>	y-axis label for coefficient time series.
<code>mean.lab</code>	Label for mean component.
<code>level.lab</code>	Label for level component.
<code>main.title</code>	Title for main effects.
<code>interaction.title</code>	Title for interaction terms.
<code>basiscol</code>	Colors for principal components if <code>plot.type = "components"</code> .
<code>coeffcol</code>	Colors for time series coefficients if <code>plot.type = "components"</code> .
<code>outlier.col</code>	Colors for outlying years.
<code>outlier.pch</code>	Plotting character for outlying years.
<code>outlier.cex</code>	Size of plotting character for outlying years.
<code>...</code>	Plotting parameters.

Value

Function produces a plot.

Author(s)

Rob J Hyndman

References

R. J. Hyndman and M. S. Ullah (2007) "Robust forecasting of mortality and fertility rates: A functional data approach", *Computational Statistics & Data Analysis*, **51**(10), 4942-4956.

R. J. Hyndman and H. Booth (2008) "Stochastic population forecasts using functional data models for mortality, fertility and migration", *International Journal of Forecasting*, **24**(3), 323-342.

R. J. Hyndman and H. L. Shang (2009) "Forecasting functional time series (with discussion)", *Journal of the Korean Statistical Society*, **38**(3), 199-221.

See Also

[ftsm](#), [forecast.ftsm](#), [residuals.fm](#), [summary.fm](#), [plot.fmres](#), [plot.ftsf](#)

Examples

```
plot(x = ftsm(y = ElNino))
plot(x = fplsr(data = ElNino), ylab1 = "Predictor score",
      ylab2 = "Response loading")
```

plot.fmres

Plot residuals from a fitted functional model.

Description

Functions to produce a plot of residuals from a fitted functional model.

Usage

```
## S3 method for class 'fmres'
plot(x, type = c("image", "fts", "contour", "filled.contour",
  "persp"), xlab = "Year", ylab = "Age", zlab = "Residual", ...)
```

Arguments

x	Generated by <code>residuals(fit)</code> , where <code>fit</code> is the output from <code>ftsm</code> or <code>fplsr</code> .
type	Type of plot to use. Possibilities are <code>image</code> , <code>fts</code> , <code>contour</code> , <code>filled.contour</code> and <code>persp</code> .
xlab	Label for x-axis.
ylab	Label for y-axis.
zlab	Label for z-axis.
...	Plotting parameters.

Value

Produces a plot.

Author(s)

Rob J Hyndman

See Also

[ftsm](#), [forecast.ftsm](#), [plot.fm](#), [plot.fmres](#), [residuals.fm](#), [summary.fm](#)

Examples

```
plot(residuals(ftsm(ElNino)), type = "filled.contour", xlab = "Month",
      ylab = "Residual sea surface temperature")
```

plot.ftsf

Plot fitted model components for a functional time series model

Description

Plot fitted model components for a fts object.

Usage

```
## S3 method for class 'ftsf'
plot(x, plot.type = c("function", "components", "variance"),
      components, xlab1 = fit$y$xname, ylab1 = "Basis function",
      xlab2 = "Time", ylab2 = "Coefficient", mean.lab = "Mean",
      level.lab = "Level", main.title = "Main effects",
      interaction.title = "Interaction", vcol = 1:3, shadecols = 7,
      fcol = 4, basiscol = 1, coeffcol = 1, outlier.col = 2,
      outlier.pch = 19, outlier.cex = 0.5,...)
```

Arguments

x	Output from forecast.ftsm .
plot.type	Type of plot.
components	Number of principal components.
xlab1	x-axis label for principal components.
xlab2	x-axis label for coefficient time series.
ylab1	y-axis label for principal components.
ylab2	y-axis label for coefficient time series.
mean.lab	Label for mean component.
level.lab	Label for level component.

main.title	Title for main effects.
interaction.title	Title for interaction terms.
vcol	Colors to use if plot.type = "variance".
shadecols	Color for shading of prediction intervals when plot.type = "components".
fcoll	Color of point forecasts when plot.type = "components".
basiscol	Colors for principal components if plot.type = "components".
coeffcol	Colors for time series coefficients if plot.type = "components".
outlier.col	Colors for outlying years.
outlier.pch	Plotting character for outlying years.
outlier.cex	Size of plotting character for outlying years.
...	Plotting parameters.

Details

When plot.type = "function", it produces a plot of the forecast functions;

When plot.type = "components", it produces a plot of the principal components and coefficients with forecasts and prediction intervals for each coefficient;

When plot.type = "variance", it produces a plot of the variance components.

Value

Function produces a plot.

Author(s)

Rob J Hyndman

References

R. J. Hyndman and M. S. Ullah (2007) "Robust forecasting of mortality and fertility rates: A functional data approach", *Computational Statistics and Data Analysis*, **51**(10), 4942-4956.

R. J. Hyndman and H. Booth (2008) "Stochastic population forecasts using functional data models for mortality, fertility and migration", *International Journal of Forecasting*, **24**(3), 323-342.

R. J. Hyndman and H. L. Shang (2009) "Forecasting functional time series (with discussion)", *Journal of the Korean Statistical Society*, **38**(3), 199-221.

See Also

[ftsm](#), [plot.fm](#), [plot.fmres](#), [residuals.fm](#), [summary.fm](#)

Examples

```
plot(x = forecast(object = ftsm(y = ElNino)))
```

plot.ftsm	<i>Plot fitted model components for a functional time series model</i>
-----------	------------------------------------------------------------------------

Description

Plot showing the basis functions in the top row of plots and the coefficients in the bottom row of plots.

Usage

```
## S3 method for class 'ftsm'
plot(x, components, xlab1 = x$y$name, ylab1 = "Basis function",
     xlab2 = "Time", ylab2 = "Coefficient", mean.lab = "Mean",
     level.lab = "Level", main.title = "Main effects",
     interaction.title = "Interaction", basiscol = 1, coeffcol = 1,
     outlier.col = 2, outlier.pch = 19, outlier.cex = 0.5, ...)
```

Arguments

x	Output from <code>ftsm</code> .
components	Number of principal components to plot.
xlab1	x-axis label for basis functions.
xlab2	x-axis label for coefficient time series.
ylab1	y-axis label for basis functions.
ylab2	y-axis label for coefficient time series.
mean.lab	Label for mean component.
level.lab	Label for level component.
main.title	Title for main effects.
interaction.title	Title for interaction terms.
basiscol	Colors for basis functions if <code>plot.type="components"</code> .
coeffcol	Colors for time series coefficients if <code>plot.type="components"</code> .
outlier.col	Colour for outlying years.
outlier.pch	Plotting character for outlying years.
outlier.cex	Size of plotting character for outlying years.
...	Plotting parameters.

Value

None. Function produces a plot.

Author(s)

Rob J Hyndman

References

R. J. Hyndman and M. S. Ullah (2007) "Robust forecasting of mortality and fertility rates: A functional data approach", *Computational Statistics and Data Analysis*, **51**(10), 4942-4956.

R. J. Hyndman and H. L. Shang (2009) "Forecasting functional time series" (with discussion), *Journal of the Korean Statistical Society*, **38**(3), 199-221.

See Also

[forecast.ftsm](#), [ftsm](#), [plot.fm](#), [plot.ftsf](#), [residuals.fm](#), [summary.fm](#)

Examples

```
plot.ftsm(ftsm(ElNino, 4), components = 2)
```

plotfpls

Plot fitted model components for a functional time series model

Description

Plot showing the basis functions of the predictors in the top row, followed by the basis functions of the responses in the second row, then the coefficients in the bottom row of plots.

Usage

```
plotfpls(x, xlab1 = x$ypred$xname, ylab1 = "Basis function", xlab2 = "Time",
         ylab2 = "Coefficient", mean.lab = "Mean", interaction.title = "Interaction")
```

Arguments

x	Output from fpls .
xlab1	x-axis label for basis functions.
ylab1	y-axis label for basis functions.
xlab2	x-axis label for coefficient time series.
ylab2	y-axis label for coefficient time series.
mean.lab	Label for mean component.
interaction.title	Title for interaction terms.

Value

None. Function produces a plot.

Author(s)

Han Lin Shang

References

R. J. Hyndman and M. S. Ullah (2007) "Robust forecasting of mortality and fertility rates: A functional data approach", *Computational Statistics and Data Analysis*, **51**(10), 4942-4956.

R. J. Hyndman and H. L. Shang (2009) "Forecasting functional time series" (with discussion), *Journal of the Korean Statistical Society*, **38**(3), 199-221.

See Also

[forecast.ftsm](#), [ftsm](#), [plot.fm](#), [plot.ftsf](#), [residuals.fm](#), [summary.fm](#)

Examples

```
ausfplsr = fplsr(Australiasmoothfertility, 2)
plotfplsr(ausfplsr)
```

quantile.fts

Quantile functions for functional time series

Description

Computes quantiles of functional time series at each variable.

Usage

```
## S3 method for class 'fts'
quantile(x, probs = c(0.25, 0.75), ...)
```

Arguments

x	An object of class <code>fts</code> .
probs	Quantile percentages.
...	Other arguments.

Value

Return quantiles for each variable.

Author(s)

Han Lin Shang

See Also

[mean.fts](#), [median.fts](#), [var.fts](#), [sd.fts](#)

Examples

```
quantile(x = ElNino)
```

`residuals.fm`*Compute residuals from a functional model*

Description

After fitting a functional model, it is useful to inspect the residuals. This function extracts the relevant information from the fit object and puts it in a form suitable for plotting with `image`, `persp`, `contour`, `filled.contour`, etc.

Usage

```
## S3 method for class 'fm'  
residuals(object, ...)
```

Arguments

<code>object</code>	Output from <code>ftsm</code> or <code>fplsr</code> .
<code>...</code>	Other arguments.

Value

Produces an object of class “fmres” containing the residuals from the model.

Author(s)

Rob J Hyndman

References

- B. Erbas and R. J. Hyndman and D. M. Gertig (2007) "Forecasting age-specific breast cancer mortality using functional data model", *Statistics in Medicine*, **26**(2), 458-470.
- R. J. Hyndman and M. S. Ullah (2007) "Robust forecasting of mortality and fertility rates: A functional data approach", *Computational Statistics & Data Analysis*, **51**(10), 4942-4956.
- R. J. Hyndman and H. Booth (2008) "Stochastic population forecasts using functional data models for mortality, fertility and migration", *International Journal of Forecasting*, **24**(3), 323-342.

See Also

[ftsm](#), [forecast.ftsm](#), [summary.fm](#), [plot.fm](#), [plot.fmres](#)

Examples

```
plot(residuals(object = ftsm(ElNino)), xlab = "Year", ylab = "Month")  
plot(residuals(object = fplsr(ElNino)), xlab = "Year", ylab = "Month")
```

`sd.fts`*Standard deviation functions for functional time series*

Description

Computes standard deviation of functional time series at each variable.

Usage

```
## S3 method for class 'fts'  
sd(x, method = c("coordinate", "FM", "mode", "RP", "RPD"),  
   trim = 0.25,...)
```

Arguments

<code>x</code>	An object of class <code>fts</code> .
<code>method</code>	Method for computing median.
<code>trim</code>	Percentage of trimming.
<code>...</code>	Other arguments.

Details

If `method = "coordinate"`, it computes coordinate-wise standard deviation functions.

If `method = "FM"`, it computes the standard deviation functions of trimmed functional data ordered by the functional depth of Fraiman and Muniz (2001).

If `method = "mode"`, it computes the standard deviation functions of trimmed functional data ordered by h -modal functional depth.

If `method = "RP"`, it computes the standard deviation functions of trimmed functional data ordered by random projection depth.

If `method = "RPD"`, it computes the standard deviation functions of trimmed functional data ordered by random projection derivative depth.

Value

A list containing `x = variables` and `y = standard deviation rates`.

Author(s)

Han Lin Shang

References

- O. Hossjer and C. Croux (1995) "Generalized univariate signed rank statistics for testing and estimating a multivariate location parameter", *Nonparametric Statistics*, **4**(3), 293-308.
- A. Cuevas and M. Febrero and R. Fraiman (2006) "On the use of bootstrap for estimating functions with functional data", *Computational Statistics & Data Analysis*, **51**(2), 1063-1074.
- M. Febrero and P. Galeano and W. Gonzalez-Manteiga (2008) "Outlier detection in functional data by depth measures, with application to identify abnormal NOx levels", *Environmetrics*, **19**(4), 331-345.

See Also

[mean.fts](#), [median.fts](#), [var.fts](#), [quantile.fts](#)

Examples

```
sd.fts(x = ElNino, method = "coordinate")
sd.fts(x = ElNino, method = "FM")
sd.fts(x = ElNino, method = "mode")
sd.fts(x = ElNino, method = "RP")
sd.fts(x = ElNino, method = "RPD")
```

summary.fm

Summary for functional time series model

Description

Summarizes a basis function model fitted to a functional time series. It returns various measures of goodness-of-fit.

Usage

```
## S3 method for class 'fm'
summary(object, ...)
```

Arguments

object	Output from ftsm or fplsr .
...	Other arguments.

Value

None.

Author(s)

Rob J Hyndman

See Also

[ftsm](#), [forecast.ftsm](#), [residuals.fm](#), [plot.fm](#), [plot.fmres](#)

Examples

```
summary(object = ftsm(ElNino))
summary(object = fplsr(ElNino))
```

var.fts

Variance functions for functional time series

Description

Computes variance functions of functional time series at each variable.

Usage

```
## S3 method for class 'fts'
var(x, method = c("coordinate", "FM", "mode", "RP", "RPD"),
    trim = 0.25,...)
```

Arguments

x	An object of class <code>fts</code> .
method	Method for computing median.
trim	Percentage of trimming.
...	Other arguments.

Details

If `method = "coordinate"`, it computes coordinate-wise variance.

If `method = "FM"`, it computes the variance of trimmed functional data ordered by the functional depth of Fraiman and Muniz (2001).

If `method = "mode"`, it computes the variance of trimmed functional data ordered by h -modal functional depth.

If `method = "RP"`, it computes the variance of trimmed functional data ordered by random projection depth.

If `method = "RPD"`, it computes the variance of trimmed functional data ordered by random projection derivative depth.

Value

A list containing $x =$ variables and $y =$ variance rates.

Author(s)

Han Lin Shang

References

O. Hossjer and C. Croux (1995) "Generalized univariate signed rank statistics for testing and estimating a multivariate location parameter", *Nonparametric Statistics*, **4**(3), 293-308.

A. Cuevas and M. Febrero and R. Fraiman (2006) "On the use of bootstrap for estimating functions with functional data", *Computational Statistics & Data Analysis*, **51**(2), 1063-1074.

M. Febrero and P. Galeano and W. Gonzalez-Manteiga (2008) "Outlier detection in functional data by depth measures, with application to identify abnormal NOx levels", *Environmetrics*, **19**(4), 331-345.

See Also

[mean.fts](#), [median.fts](#), [sd.fts](#), [quantile.fts](#)

Examples

```
var.fts(x = ElNino, method = "coordinate")
var.fts(x = ElNino, method = "FM")
var.fts(x = ElNino, method = "mode")
var.fts(x = ElNino, method = "RP")
var.fts(x = ElNino, method = "RPD")
```

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